

# A review of machine learning-driven studies of tearing modes

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Tearing modes in tokamaks reduce plasma confinement and lead to disruptions

Like fusion output, their severity generally increases with plasma pressure.

Tokamak tearing research:

- find viable tearing-free pilot plant scenarios
- predict and prevent tearing onset in real time

How has machine learning (ML) have furthered these goals?

#### Background

- Tearing-to-disruption
- Identifying tearing modes
- Tearing physics to motivate machine learning

#### **Review of ML-driven tearing studies**

**Summary and future directions** 

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#### **Tearing modes (TMs) in tokamaks have periodic modal structure**



Simulated islands in DIII-D

#### Tearing modes:

- have m,n poloidal and toroidal Fourier mode numbers
- occur on rational surfaces where field lines close on themselves with helicity q = m/n

#### **Tearing modes damage confinement**

Simulated islands in DIII-D



Particles adhere to field lines:

Nested flux surfaces  $\rightarrow$  particles well confined

Reconnection  $\rightarrow$  island fields have finite radial width

 $\rightarrow\,$  fast radial transport and heat loss



#### Rotating island:



Rotating island:

$$\rightarrow$$
 drag via  $\nabla \times E = -\frac{\partial B}{\partial t}$ 



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 $\rightarrow$  overlapping island chains  $\Leftrightarrow$  chaos  $\Leftrightarrow$  disruption



Rotating island:

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 drag via  $\nabla \times \boldsymbol{E} = -\frac{\partial \boldsymbol{B}}{\partial t}$ 

 $\rightarrow$  mode locking, accelerated growth

→ overlapping island chains ⇔ chaos ⇔ disruption

Leading cause of disruptions at JET<sup>[1]</sup>

18% of disruptions at DIIID due to TMs locking<sup>[2]</sup>

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### Tearing modes can identified with diagnostic coils

Rotating tearing mode

- $\rightarrow$  time varying 3D field
  - $\rightarrow$  diagnostic coils experience oscillating current



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Preprocessing step: fast fourier transform coil signals





Step i: Filter signal noise

#### Preprocessing step: fast fourier transform coil signals





Step i:Filter signal noiseStep ii:Isolate cohesive signals

Preprocessing step: fast fourier transform coil signals







<sup>1</sup>E d D Zapata-Cornejo et al 2024 PPCF 66 095016 <sup>2</sup>E d D Zapata-Cornejo. HAL Thesis, AMU, 2024. <u>(NNT : 2024AIXM0376)</u>. <u>(tel-04904999)</u>, under development at MIT-PSFC

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- Step i: Filter signal noise
- Step ii: Isolate cohesive signals
- Step iii: Identify toroidal mode n using phase differences

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### Tokamak tearing physics can motivate and contextualise an ML approach

Predicting tearing stability is hard...

- for real time control, or scenario design

Why?

Tokamak tearing onset is moderated by multiple coupled, chaotic mechanisms

The dynamics are sensitive to gradients of equilibrium quantities

What is the simplest model that explains this, and is consistent with experiment?

# A minimal description of tokamak tearing physics:

- 1. Nonlinear tearing dynamics:
  - modified Rutherford equation (MRE)
- 2. 'Seeding' and differential plasma rotation
- 3. Mode rotation as confounding variable

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 $\frac{k_0}{n^*}\frac{dw}{dt} = \Delta'^* + \Delta_{nc} + \Delta_{GGJ} + \Delta_{pol} + \dots$ 

TMs can be modelled using the modified Rutherford equation (MRE) [1][2][3][4]:

Predicts the dynamics of a single-helicity tearing mode after it has exceeded the characteristic resistive linear layer width  $\delta_r$ 

[1] Hegna, PoP (1999)
[2] Schlutt & Hegna, PoP (2012)
[3] La Haye, PoP (2006) 25
[4] La Haye et al., NF (2022)

### TMs can be modelled with MRE: $\frac{k_0}{\eta *} \frac{dw}{dt} = \Delta'^* + \Delta_{nc} + \Delta_{GGJ} + \Delta_{pol} + \dots$



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Go through term-by-term

 $\frac{k_0}{\eta *} \frac{dw}{dt}$  $= \Delta'^* + \Delta_{nc} + \Delta_{GGJ} + \Delta_{pol} + \dots$ 

$$\Delta'^* = \Delta' |w/2|^{-\alpha_-} \sqrt{-4D_I}$$

Equilibrium ideal outer-region stability

 $\frac{k_0}{n^*}\frac{dw}{dt} = \Delta'^* + \Delta_{nc} + \Delta_{GGJ} + \Delta_{pol} + \dots$ 

$$\Delta'^* = \Delta' |w/2|^{-\alpha_-} \sqrt{-4D_I}$$

Equilibrium ideal outer-region stability

- Toroidal  $\Delta^{\prime_{[1,2]}}$
- Finite-pressure, general toroidal geometry<sup>[3]</sup>
- Generally stabilising

TMs can be modelled with MRE:  $\frac{k_0}{n*}\frac{dw}{dt} = \Delta$ 

$$\frac{k_0}{\eta *} \frac{dw}{dt} = \Delta'^* + \Delta_{nc} + \Delta_{GGJ} + \Delta_{pol} + \dots$$

$$\Delta_{GGJ} = \frac{1}{w + k_3 w_d} \frac{k_1 D_R}{\alpha_+ - H} \qquad D_R = D_I + (H - 1/2)$$

#### Local field-line curvature term<sup>[2,3]</sup>

- Generally stabilising
- Small

### Neoclassical term drives TM growth:

$$\frac{k_0}{\eta *}\frac{dw}{dt} = \Delta'^* + \Delta_{nc} + \Delta_{GGJ} + \Delta_{pol} + \dots$$

$$\Delta_{nc} = \frac{w}{w^2 + 2k_1 w_d^2} k_1 D_{nc}$$

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Neoclassical drive 
$$D_{nc} \sim \frac{J_{bs}}{J_{\parallel}} \frac{q}{q'}$$
 dominates at island-widths seen during experiment: [4]

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mag. island  $\rightarrow$  no pressure gradient  $\rightarrow$  lose local bootstrap current  $\rightarrow$  drives reconnection

### TMs require a seed island:

$$\frac{k_0}{\eta *}\frac{dw}{dt} = \Delta'^* + \Delta_{nc} + \Delta_{GGJ} + \Delta_{pol} + \dots$$

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requires 'seed' island of width  $w \sim w_d$ , otherwise cross-field (turbulent) transport maintains pressure gradient across island chain [5,6]

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[4] La Haye, PoP (2006) 35
 [5] Fitzpatrick, PoP (1995)
 [6] Schlutt & Hegna, PoP (2012)

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Fast transient perturbed field (eg. ideal m,n = 1,1 'sawteeth' instability)

 $\rightarrow$  short-lived 3D fields

 $\rightarrow$  forced reconnection at core rational surfaces

^Implicit time scale separation:

- tearing modes slow reconnection
- sawteeth 'seed' fast reconnection

Relative toroidal rotation

between rational surfaces

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 $\rightarrow$  perturbed fields screened out

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2/1 tearing onset vs differential rotation



Empirical probability [%]

Relative toroidal rotation

between rational surfaces

 $\rightarrow$  perturbed fields screened out

### q = 1, 2 surfaces decoupled

 $\rightarrow$  no seeding from sawteeth

2/1 tearing onset vs differential rotation



Bardóczi et al., PoP (2023)

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Ion polarisation current can strongly stabilise TMs at small island widths

- two-fluid effect

Relies on relative rotation between island chain and frame of zero radial field [1,2,3]

[1] Waelbroeck et al., PRL (2001)
[2] Connor et al., PoP (2001) 46
[3] Waelbroeck., PRL (2005)

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Chaotic dynamics motivates a statistical/ML approach

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Bardóczi et al. 2023<sup>[1]</sup> - what plasma variables have the most influence on TM onset?

Using 14260 shots on the DIII-D tokamak:

Calculated dependence of 2/1 TM onset probability on various plasma parameters:

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Ranked param. importance by variation in probability minus error



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Most important terms:

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⇔ bootstrap drive

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- $\Leftrightarrow$  seeding from 3/2 modes

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[1] Bardóczi et al., PoP (2023), [2] Bardóczi et al., NF (2023)

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2/1 onset consistent with time-independent random process

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2/1 onset consistent with <sup>1</sup> time-independent random process **Depends on scenario!** 

[1] Bardóczi et al., PoP (2023), [2] Bardóczi et al., NF (2023)

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- Statistical analyses of TM onset
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#### Machine learning can be used to warn of impending tearing modes

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List of relevant publications:

Buttery et al. NF (2004)

Fu et al. PoP (2020)

Olofsson et al. JPP (2022)

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Farre-Kaga et al. 2025 Clofsson et al. 2022

Survival analysis

- statistical framework for Pr (event | time)
- time series data as inputs

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  - Deep Survival Machine ++

[1] Keith et al., J.Fus.En. (2024), [2] Nagpal et al., ArXiv (2021)

Farre-Kaga et al. 2025 - Predicting tearing onset with a Deep Survival Machine<sup>[1,2]</sup> Olofsson et al. 2022

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kinetic DIII-D equilibria rapidly reconstructed with ML<sup>[3]</sup>

- rotation, density, temperature

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 $\rightarrow$  input:

kinetic DIII-D equilibria rapidly reconstructed with ML<sup>[3]</sup>

- rotation, density, temperature
- $\rightarrow$  captured 90% of TMs with false alarm rate of 20% @ 900ms avg. warning time<sup>[4]</sup>



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[1] Keith et al., J.Fus.En. (2024), [2] Nagpal et al., ArXiv (2021), [3] Shousha et al., NF (2023), [4] Farre-Kaga et al. ArXiv (2025)

Farre-Kaga et al. 2025 - Predicting tearing onset with a Deep Survival Machine Olofsson et al. 2022 - Tearing onset can be predicted from equilibrium data alone

Trained using 18 026 DIII-D shots

Inputs:

- Ideal MHD mag. energy distribution
- applied principal component analysis to reduce dimensionality
- no rotation, temperature, density etc.

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#### Magnetic energy principal components



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#### Machine learning can be used to predict TM onset

Buttery et al. 2004 Fu et al. 2020 Olofsson et al. 2022 Bardóczi et al. 2023 Seo et al. 2023 Farre-Kaga et al. 2025

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Fu et al. 2020<sup>[1]</sup> Seo et al. 2024<sup>[2]</sup> Rothstein, Farre-Kaga et al. 2025<sup>[3]</sup>

Fu et al.  $2020^{[1]}$ Seo et al.  $2024^{[2]}$ Rothstein, Farre-Kaga et al.  $2025^{[3]}$  Tearability-actuated beam heating for tearing avoidance

Fu et al. 2020<sup>[1]</sup>

Seo et al. 2024<sup>[2]</sup>

Rothstein, Farre-Kaga et al. 2025<sup>[3]</sup> Tearability-actuated beam heating for tearing avoidance ML multi-actuator control to maximise  $\beta$  while avoiding TMs

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Fu et al. 2020<sup>[1]</sup>

Seo et al. 2024<sup>[3]</sup> Tearability-actuated neutral beams for tearing avoidance

Multi-actuator control to maximise  $\beta$  while avoiding TMs - uses reinforcement learning

Rothstein, Farre-Kaga et al. 2025<sup>[2]</sup> Tearability-actuated electron cyclotron current drive response to maximise current drive efficiency while avoiding TMs

#### ML can be used to control the plasma to avoid TM onset

**Proof of concept**  $\rightarrow$  **completed** 

Fu et al. 2020 Seo et al. 2024 Rothstein et al. 2025

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Next step: Stress-testing ML control algorithms for pilot-plant applications

Fu et al. 2020 Seo et al. 2024 Rothstein et al. 2025

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Ranking impact on TM onset:

→ how much prediction accuracy fell upon removal

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Corroborated ordering from empirical probability variance

Physics-determinants of 2/1 onset

variable	#ML impact	# ΔΡ-σ <sub>P</sub> :
Plasma beta	1	1

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Bootstrap current	2	11

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variable #ML impact # ΔΡ-σ<sub>P</sub>: Plasma beta 1 1 2 11 Bootstrap current 3 n = 2 mag. signal 4 3 q = 1, 2 differential 4 rotation

Physics-determinants of 2/1 onset

Bardóczi et al. 2023<sup>[1]</sup> - what plasma variables have the most influence on TM onset?

Farre-Kaga et al. 2025<sup>[2]</sup> Olofsson et al. 2025<sup>[3]</sup> Benjamin et al. 2025<sup>[4]</sup>

Shapley analysis: Allows physics-based interpretation of logic encoded in ML algorithms

^see our poster

#### Background

- Tearing-to-disruption
- Identifying tearing modes
- Tearing physics to motivate machine learning

#### **Review of ML-driven tearing studies**

**Summary and future directions**
### Summarising the impact of ML on tearing research in tokamaks

Tokamak tearing physics involves coupled, multi-scale dynamics, & chaos

- this motivates a data-driven approach w. statistics and ML

ML has been able to:

- 1. identify stability trends
- 2. predict tearing onset
- 3. control the plasma to avoid tearing modes in real time (proof of concept)

Tokamak tearing physics involves coupled, multi-scale dynamics, & chaos

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ML has been able to:

sensitive to diagnostic suit<sup>[1]</sup>

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rapid & effective actuators:

- neutral beams
- electron cyclotron current drive

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 $\rightarrow$  limit diagnostic suite

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#### **SOLUTION?**



#### We propose an increased focus on tearing-free scenarios

Let's find the intersection\* of tearing-stable scenarios and fusion pilot-plants

Method:

- Apply ML to a community-driven, multi-machine tearing mode database

#### We propose an increased focus on tearing-free scenarios

Let's find the intersection\* of tearing-stable scenarios and fusion pilot-plants

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Interested in stabilising fully-inductive scenarios? Come see:

### 'Macroscopic trends of linear and neoclassical tearing stability in high-field H-mode tokamak pilot plants'

Work supported by Commonwealth Fusion Systems and U.S. Department of Energy FES under Award DE-SC0014264.

#### **BACKUP SLIDES**

Farre-Kaga et al. 2025<sup>[1]</sup> - ML confirms temperature gradients destabilise TMs

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Tearability predictor for 2/1 mode onset trained on 6050 DIII-D shots

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Shapley analysis:

Correlates input values to Tearability predictions, shifted by mean Tearability

Farre-Kaga et al.  $2025^{[1]}$  - ML confirms temperature gradients destabilise TMs Benjamin et al.  $2025^{[2]}$  -  $\Delta$ ' is well constrained by MRE curvature stabilisation term

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Farre-Kaga et al.  $2025^{[1]}$  - ML confirms temperature gradients destabilise TMs Benjamin et al.  $2025^{[2]}$  -  $\Delta$ ' is well constrained by MRE curvature stabilisation term

Monte-Carlo generated 14667 tokamak inductive pilot-plant equilibria

Calculated toroidal  $\Delta$ ' values using resistive DCON<sup>[3]</sup>

Trained an ML  $\Delta$ ' predictor using local tearing physics terms

Farre-Kaga et al.  $2025^{[1]}$  - ML confirms temperature gradients destabilise TMs Benjamin et al.  $2025^{[2]}$  -  $\Delta$ ' is well constrained by MRE curvature stabilisation term



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Farre-Kaga et al. 2025<sup>[1]</sup> Benjamin et al. 2025<sup>[2]</sup> Olofsson et al. 2025<sup>[3]</sup>

[1] Farre-Kaga et al., arXiv:2502.20294v1 (2025) [2] Manuscript in prep. [3] Olofsson et al., NF (2025)

MIT's Alcator C-Mod tokamak cross-section





i. pick a point in frequency/time space



MIT's Alcator C-Mod tokamak cross-section



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i. pick a point in frequency/time space



MIT's Alcator C-Mod tokamak cross-section



i. pick a point in frequency/time spaceii. compute phase differences across all probes



MIT's Alcator C-Mod tokamak cross-section



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i. pick a point in frequency/time spaceii. compute phase differences across all probesii. compare with expected phase differences for set m, n modes



MIT's Alcator C-Mod tokamak cross-section



Neural network (NN):

Layers of nonlinear activation functions that combine and transform inputs parameters into an output that minimises prediction error

Parameters used in network

 $\beta_{\rm N}, \tau_{\rm sawtooth}, \rho_{\rm i\phi}^*$ 

Neural network (NN):

- Inputs are passed through `layers' of nonlinear activation functions that combine and transform them
- Produces an output that minimises prediction error

Parameters used in network

 $\beta_{\rm N}, \tau_{\rm sawtooth}, \rho^*_{\rm i\phi}$ 

Neural network (NN):

Layers of nonlinear activation functions that combine and transform inputs parameters into an output that minimises prediction error

output = time to TM onset at set time intervals error =  $\Sigma$  (predicted - actual time to onset)<sup>2</sup>

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Parameters used in network	Values of test residual	Number of errors
$eta_{ m N}, au_{ m sawtooth}, ho_{ m i\phi}^{*}$	34.31	6

output = time to TM onset at set time intervals error =  $\Sigma$  (predicted - actual time to onset)<sup>2</sup>



### Buttery et al. 2004: Sawtooth period, $\beta$ are important for prediction

Parameters used in network	Values of test residual	Number of errors
$\beta_{\rm N}, \tau_{\rm sawtooth}, \rho_{\rm i\phi}^*$	34.31	6
$\beta_{\rm N}, \tau_{\rm sawtooth}$	34.41	7
$\beta_{\rm N}, \rho_{\rm i\phi}^*$	35.68	9
$\beta_{\rm N}$	35.87	11
$\rho^*_{i\phi}$	37.45	10
$ au_{\rm sawtooth}$	48.85	14
$\tau_{\text{sawtooth}}, \rho_{\text{i}\phi}^*$	37.46	9



### Buttery et al. 2004: Shorter sawtooth period $\rightarrow$ higher $\beta$ limit

Parameters used in network	Values of test residual	Number of errors
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Tearing hazard function: Average TM onset frequency as a function of plasma state

Converted into a simple optimisation problem

Trained using a boosted tree model:

Tree:

- subdivides input space into rectangular regions
- makes prediction based on average of training data in each region

Boosted tree:

Iteratively constructs trees and sums their predictions

Finding average TM onset frequency as a function of DIII-D tearing physics terms

Quantity	Text	Description
$\overline{\rho_q \Delta'}$	rdpr21	Delta-prime proxy
$D_R^{\rm apx} \rho_q / w_{\rm sml}$	merc21	MRE Mercier term
$2\sqrt{\epsilon}L_q\rho_q/(3L_{pe}w_{\rm sml})$	boot21	MRE bootstrap term
$-(\mathrm{d}\omega/\mathrm{d} ho)L_s au_A$	nfs21	Norm. flow shear
$\hat{\rho}_q = \rho_q / \rho_b$	rho21	Norm. radial q-pos.
$\ell_i$	elli	Internal inductance
$q_{95}$	q95	q at 95% of pol. flux
$\beta_p$	betap	Poloidal $\beta$
$n/n_G$	grwdens	Greenwald density
$\mu_0 I_{pl}/(\rho_b B_0)$	iphat	Norm. current
$ au_{\mathrm{crt}} P_{\mathrm{bol}} / (W_p + W_k)$	pradhat	Radiated power index
$100   imes  \omega  au_A$	alfvprc	Norm. avrg. rotation

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Iterative feature selection:



Finding average TM onset frequency as a function of DIII-D tearing physics terms

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Iterative feature selection:



#### Sorted elimination path (100x)

Finding average TM onset frequency as a function of DIII-D tearing physics terms

Three most important terms:

- 1. flow shear
- 2. poloidal beta
- 3. MRE bootstrap current term

Finding average TM onset frequency as a function of DIII-D tearing physics terms

Three most important terms:

- 1. flow shear
- 2. poloidal beta
- 3. MRE bootstrap current term

Delta-prime proxy **not** important:

- 'equilibrium' value doesn't vary significantly/not dominant term?
- high-m formulation not appropriate?
- obscured by error?

**Oloffson et al. 2018: Low or reversed flow shear is extremely destabilising** 


Fu et al. 2020 - How to construct a tearing onset predictor

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Time series of training inputs supplied to a ML fitting algorithm

Fu et al. 2020

- How to construct a tearing onset predictor

Time series of training inputs supplied to a ML fitting algorithm

Define output 'Tearability'  $\in [0,1]$ 



Fu et al. 2020

- How to construct a tearing onset predictor

Time series of training inputs supplied to a ML fitting algorithm

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Trained on 1970 shots on DIII-D w. 0D physics quantities



Fu et al. 2020

- How to construct a tearing onset predictor

Time series of training inputs supplied to a ML fitting algorithm

Define output 'Tearability' ∈ [0,1]

Trained on 1970 shots on DIII-D w. 0D physics quantities

Able to correctly detect 90% of TMs with a false alarm rate of 8% > 400ms avg. warning time



Applies deep reinforcement learning:

Neural network-based plasma controller trained to maximise reward R based on its actions:

$$R = \begin{cases} \beta_{N'} & \text{if } T < k \\ k - T, & \text{otherwise} \end{cases}$$

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Dynamical model: Seo at al., (2023)

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Requires dynamical model for plasma response given an action...

Dynamical model: Seo at al., (2023)

Time series data fed to neural network Predicts Tearability  $\in [0,1] \& \beta_N$  at time t + 25ms

Inputs:

- current diagnostic information
- future actuator response
- 8505 DIII-D shots, 639 555 time slices

$$R = \begin{cases} \beta_{\rm N}, & \text{if } T < k \\ k - T, & \text{otherwise} \end{cases}$$



MIT Plasma Science & Fusion Center